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We hope you have found this information useful. If you experience any problems in following the instructions above, please contact the Beyond team at and we will do our best to help with your query.

## Your turn

Solve each of the following equations:

1. $12 x+2=2 x-28$

$$
\begin{aligned}
10 x & =-30 \\
x & =-3
\end{aligned}
$$

8. $3 x+3=x+8$
$2 x=5$
$x=2.5$
9. $4 x-2=12-3 x$
$7 x=14$
$x=2$
10. $12 x+3=9 x-12$
$3 x=-15$
$x=-5$
11. $9 x+12=6 x+14$
$3 x=2$
$x=\frac{2}{3}$
12. $15 x-45=9 x-9$

$$
\begin{aligned}
6 x & =36 \\
x & =6
\end{aligned}
$$

11. $5(x+3)=3(x+9)$

$$
\begin{aligned}
5 x+15 & =3 x+27 \\
2 x & =12 \\
x & =6
\end{aligned}
$$

5. $11 x+4=3 x-12$

$$
\begin{aligned}
8 x & =-16 \\
x & =-2
\end{aligned}
$$

12. $8(x-1)=4(x+3)$

$$
\begin{aligned}
8 x-8 & =4 x+12 \\
4 x & =20 \\
x & =5
\end{aligned}
$$

$6 x=15$

$$
x=2.5
$$

13. $\frac{6 x+1}{2}=2 x+3$

$$
6 x+1=2(2 x+3)
$$

7. $5 x+2=16-2 x$
$7 x=14$
$x=2$

$$
\begin{aligned}
6 x+1 & =4 x+6 \\
2 x & =5 \\
x & =2.5
\end{aligned}
$$

14. $\frac{5 x+2}{3}=x+2$
$5 x+2=3(x+2)$
$5 x+2=3 x+6$
$2 x=4$
$x=2$
15. $3+2 x=\frac{1}{2}(7 x-18)$
$3+2 x=3.5 x-9$
$12=1.5 x$
$8=x$
16. $3 x-2=\frac{10 x+1}{4}$

$$
\begin{aligned}
4(3 x-2) & =10 x+1 \\
12 x-8 & =10 x+1 \\
2 x & =9 \\
x & =4.5
\end{aligned}
$$

## Challenge

The diagram shows a rectangle.

a. Explain why $5 x+2=7 x-9.5$

The opposite sides of a rectangle have the same length.
b. Solve $5 x+2=7 x-9.5$
$2 x=11.5$
$x=5.75$
c. Use your answer to part (b) to work out the perimeter of the rectangle.
$5 \times 5.75+2=30.75 \mathrm{~cm}$
$7 \times 5.75-9.5=30.75 \mathrm{~cm}$
$30.75+30.75+5.75+5.75=73 \mathrm{~cm}$

## Solving Linear Equations with Variables on Both Sides

## Prior Knowledge:

- Solving equations with the variable on one side
- Expanding brackets

Solving equations means to find the value of $x$ (or whatever letter is used) that makes the equation true. To do this, you will have to rearrange the equation to get $x$ (or whatever letter is used) on its own.

Rather than using trial and error or guessing the value of $x$, it is best to keep rearranging the equation until you get the ' $x=$ ' on one side. There are a few important things to remember when rearranging.

1) You must always do the same thing to both sides of the equation.
2) To 'get rid' of something, do the opposite (use its inverse).

- The inverse of + is - and the inverse of - is + .
- The inverse of $x$ is $\div$ and the inverse of $\div$ is $\times$.

3) Finally, you must keep going until you have a letter on its own.

Equations can have unknowns or a variable on both sides of the equation.

## Example 1

Solve the following equation: $8 x+2=3 x+12$
Collect all the terms containing $x$ on one side and all the terms which don't on the other. It doesn't matter which order you start in, so long as you systematically move one term at a time. It's a good idea to write down what you're doing at every stage - put it in brackets next to the equation to help you see the calculations you are doing.

Let's start by moving the $3 x$. To do this, you must subtract $3 x$ from both sides of the equation.

$$
\begin{aligned}
& 8 x+2=3 x+12 \\
&(-3 x)^{8 x+} \\
& 5 x+2=12
\end{aligned}
$$

Now, you are able to move the 2 to the other side by subtracting it from both sides of the equation.

$$
5 x+2=12
$$

$(-2) \quad(-2)$

$$
5 x=10
$$

Finally, divide by 5 to get the ' $x=$ ' on the one side:

```
    5x=10
(\div5) (\div5)
    x=2
```


## Example 2

Solve the following equation: $\frac{4 x-3}{5}=x-2$
Start by multiplying both sides by 5 .
(×5) $\begin{aligned} \frac{4 x-3}{5} & =x-2 \\ 4 x-3 & =5(x-2)\end{aligned}(\times 5)$
Then, expand the bracket.
$4 x-3=5 x-10$

Now, you are able to solve your equation.

$$
\begin{aligned}
4 x-3 & =5 x-10 \\
(-4 x) & -3 \\
(+10) & -3-10 \\
& \\
7 & =x \text { (which is the same as } x=7)
\end{aligned}
$$

## Your turn

Solve each of the following equations:

1. $12 x+2=2 x-28$

2. $4 x-2=12-3 x$

3. $12 x+3=9 x-12$

4. $15 x-45=9 x-9$

5. $3 x+3=x+8$

6. $8 x+40=3 x+5$

7. $9 x+12=6 x+14$

8. $5(x+3)=3(x+9)$

9. $8(x-1)=4(x+3)$

10. $\frac{6 x+1}{2}=2 x+3$

11. $\frac{5 x+2}{3}=x+2$

12. $3 x-2=\frac{10 x+1}{4}$
$\square$
13. $3+2 x=\frac{1}{2}(7 x-18)$

## Challenge

The diagram shows a rectangle.

a. Explain why $5 x+2=7 x-9.5$

b. Solve $5 x+2=7 x-9.5$

c. Use your answer to part (b) to work out the perimeter of the rectangle.
$\square$

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$$
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& 5 x+2=12
\end{aligned}(-3 x)
$$

Now, you are able to move the 2 to the other side by subtracting it from both sides of the equation.

$$
5 x+2=12
$$

$(-2) \quad(-2)$

$$
5 x=10
$$

Finally, divide by 5 to get the ' $x=$ ' on the one side:

```
    5x=10
(\div5) (\div5)
    x=2
```


## Example 2

Solve the following equation: $\frac{4 x-3}{5}=x-2$
Start by multiplying both sides by 5 .
(×5) $\begin{aligned} \frac{4 x-3}{5} & =x-2 \\ 4 x-3 & =5(x-2)\end{aligned}(\times 5)$
Then, expand the bracket.
$4 x-3=5 x-10$

Now, you are able to solve your equation.

$$
\begin{aligned}
& 4 x-3=5 x-10 \\
&(-4 x)^{4 x}-3 \\
&(+10) \quad-3-10 \quad(-4 x) \\
& \\
& 7=x \text { (which is the same as } x=7)
\end{aligned}
$$

## Your turn

Solve each of the following equations:

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$\qquad$
$\qquad$
$\qquad$
2. $4 x-2=12-3 x$
3. $10 x+19=4 x+34$
$\qquad$
$\qquad$
$\qquad$
4. $12 x+3=9 x-12$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
5. $15 x-45=9 x-9$
$\qquad$
6. $3 x+3=x+8$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
7. $8 x+40=3 x+5$
$\qquad$
$\qquad$
$\qquad$
8. $9 x+12=6 x+14$
$\qquad$ 16. $3+2 x=\frac{1}{2}(7 x-18)$
$\qquad$
$\qquad$
9. $5(x+3)=3(x+9)$
$\qquad$
$\qquad$
$\qquad$

## Challenge

The diagram shows a rectangle.

a. Explain why $5 x+2=7 x-9.5$
$\qquad$
$\qquad$
b. Solve $5 x+2=7 x-9.5$
$\qquad$
$\qquad$
c. Use your answer to part (b) to work out the perimeter of the rectangle.
$\qquad$
$\qquad$
$\qquad$

